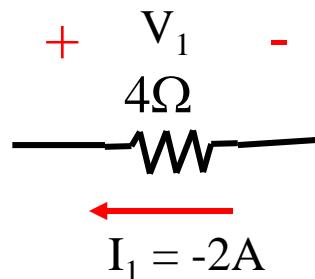


$$\mathbf{V}_1 = +\mathbf{I}_1 \mathbf{R}$$

$$\mathbf{V}_1 = +(2\mathbf{A})(4\Omega)$$

$$\mathbf{V}_1 = +8\mathbf{v}$$

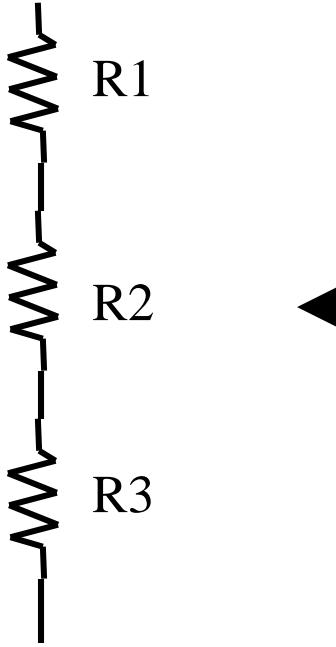


$$\mathbf{V}_1 = -\mathbf{I}_1 \mathbf{R}$$

$$\mathbf{V}_1 = -(-2\mathbf{A})(4\Omega)$$

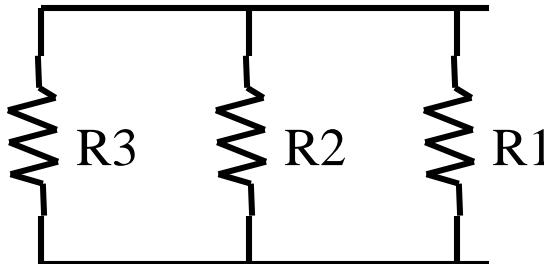
$$\mathbf{V}_1 = +8\mathbf{v}$$

Series



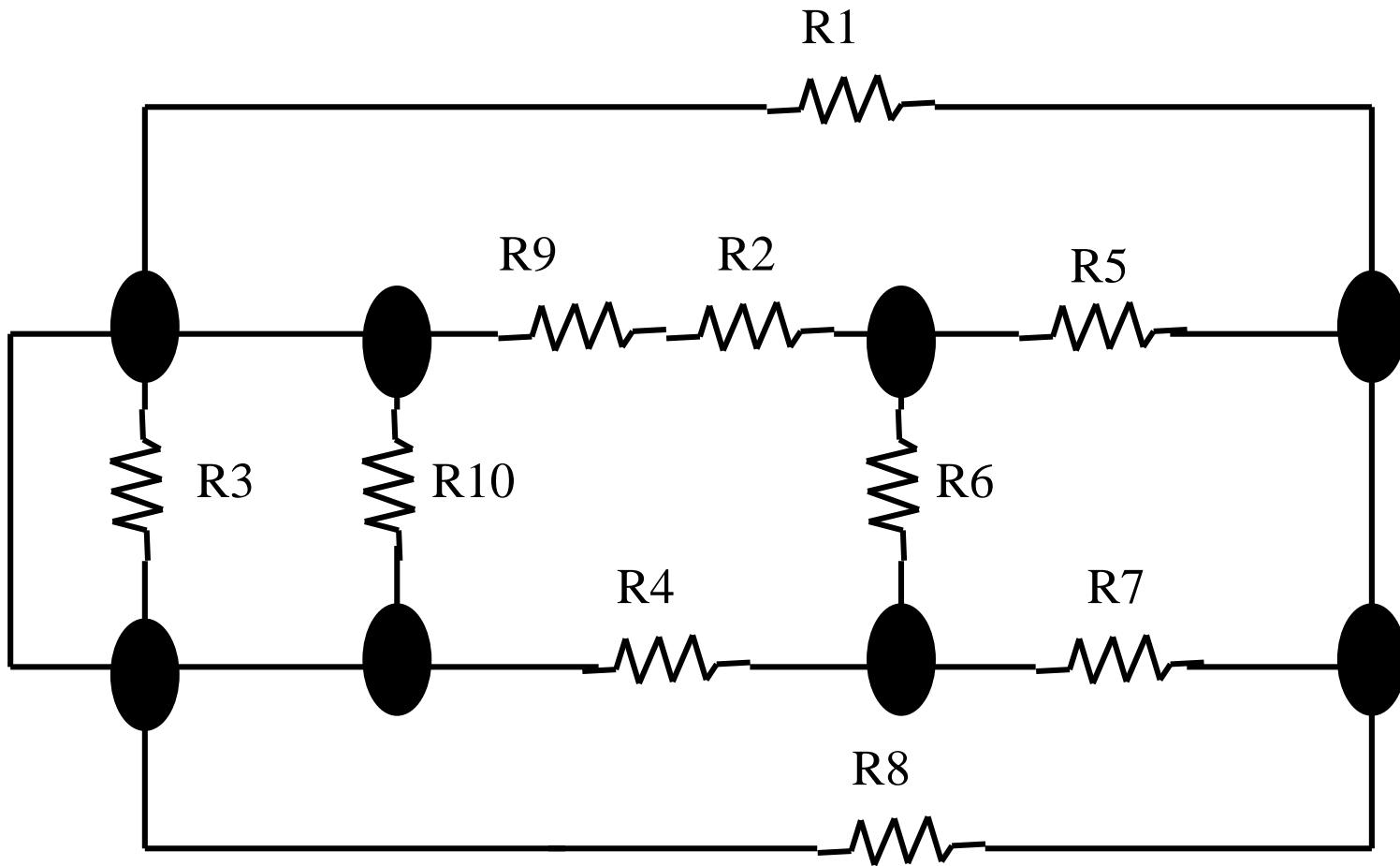
$$R_{eq} = R1 + R2 + R3$$

Parallel



$$\frac{1}{R_{eq}} = \frac{1}{R1} + \frac{1}{R2} + \frac{1}{R3}$$

~~1~~



$R_2, R_9 -$

$R_2, R_5 -$

$R_5, R_7 -$

$R_1, R_8 -$

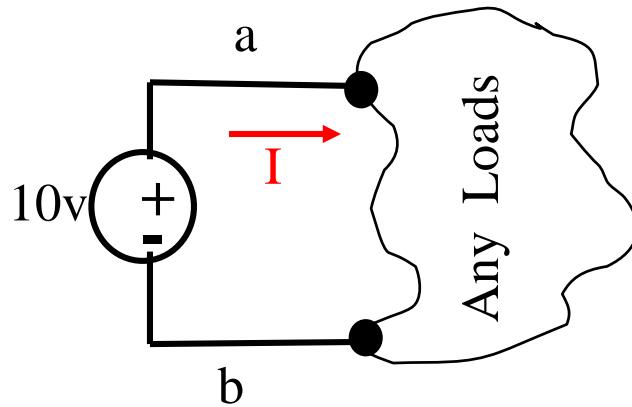
$R_4, R_7 -$

$R_6, R_7 -$

$R_3, R_{10} -$

$R_3, R_8 -$

Ideal Voltage Source

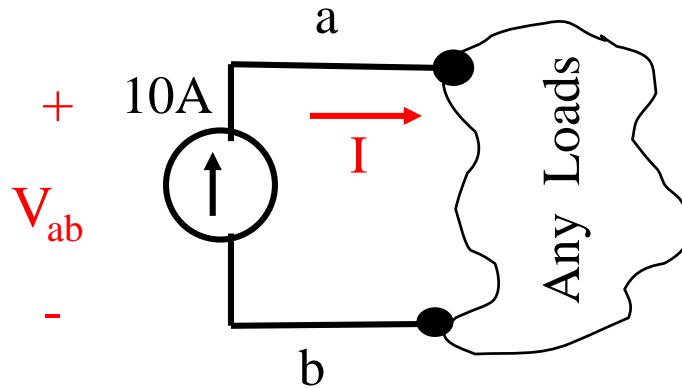


$$V_{ab} = ?$$

$$I = ?$$

Ideal Current Source

$$V_{ab} = ?$$



$$I = ?$$

- Kirchhoff's Current Law (**KCL**)
- Kirchhoff's Voltage Law (**KVL**)

Kirchhoff's Current Law (**KCL**)

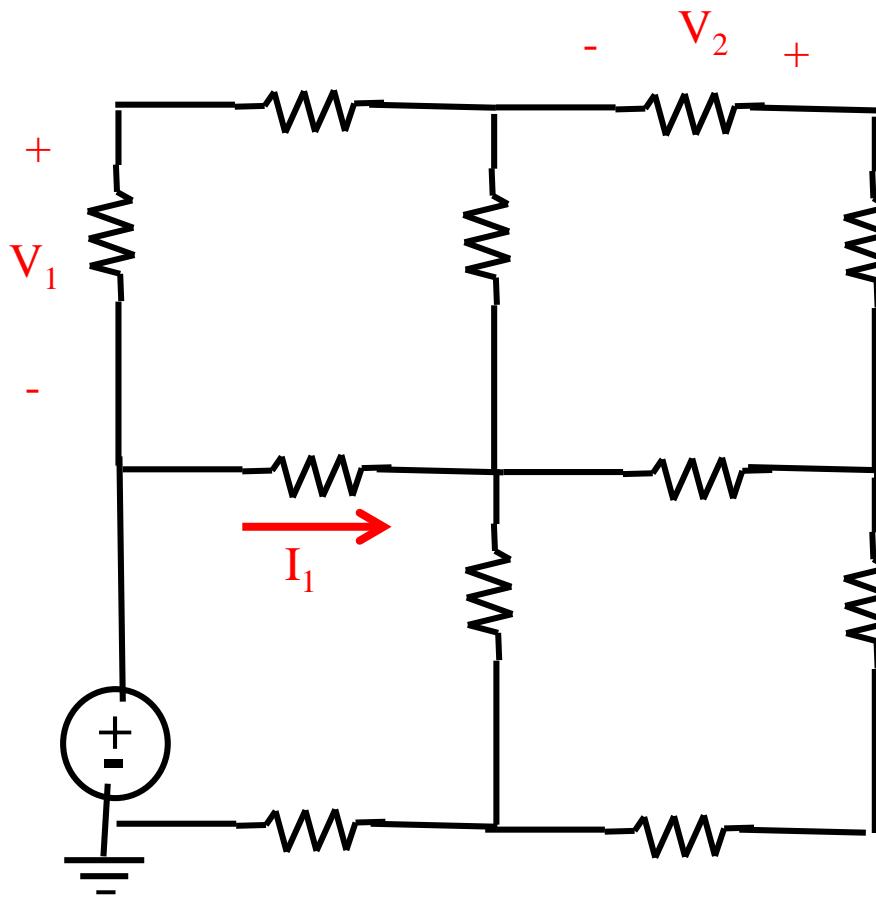
$$\sum I = 0 \quad \text{OR} \quad \sum I_{in} = \sum I_{out}$$

-- at any nodes
-- conservation of charge

Kirchhoff's Voltage Law (**KVL**)

$$\sum V = 0$$

-- at any closed loop
-- conservation of energy



$$V_1 = ?$$

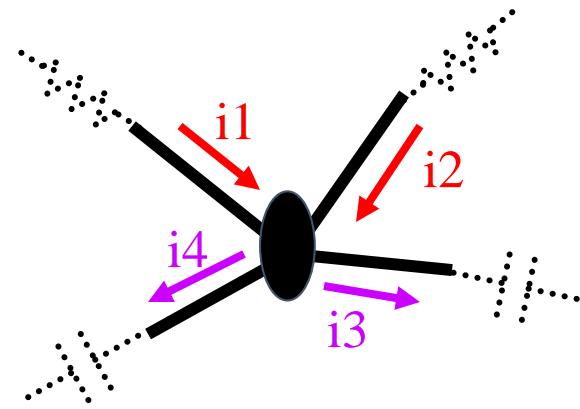
$$V_2 = ?$$

$$I_1 = ?$$

$$V = IR$$

$$\sum I = 0$$

$$\sum V = 0$$



Kirchhoff's Current Law (KCL)

Case I

$$\sum I_{in} = \sum I_{out}$$

$$i_1 + i_2 = i_3 + i_4$$

in *out*

Case II

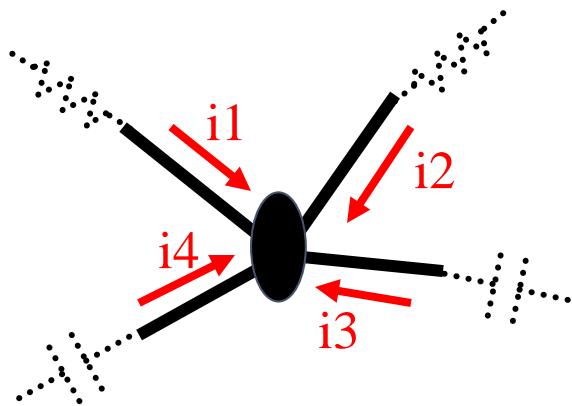
$$\sum I = 0$$

$$i_1 + i_2 + (-1)i_3 + (-1)i_4 = 0$$

Case III

$$(-1)i_1 + (-1)i_2 + i_3 + i_4 = 0$$

Ex.



$$\sum I_{in} = \sum I_{out}$$

$$i_1 + i_2 + i_3 + i_4 = ?$$

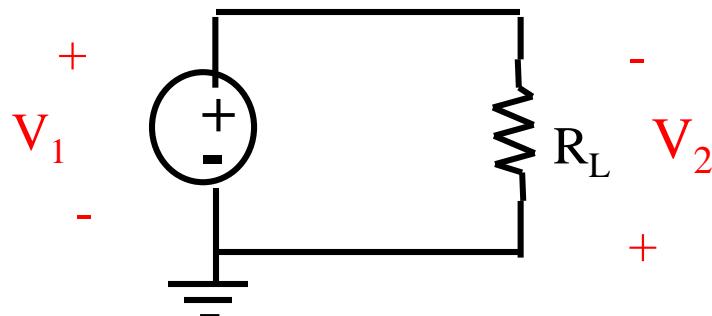
in *out*

$$i_1 + i_2 + i_3 + i_4 = 0$$

$$(+3) + (+2) + (-4) + (-1) = 0$$

$$(-3) + (-2) + (+4) + (+1) = 0$$

Kirchhoff's Voltage Law (KVL)

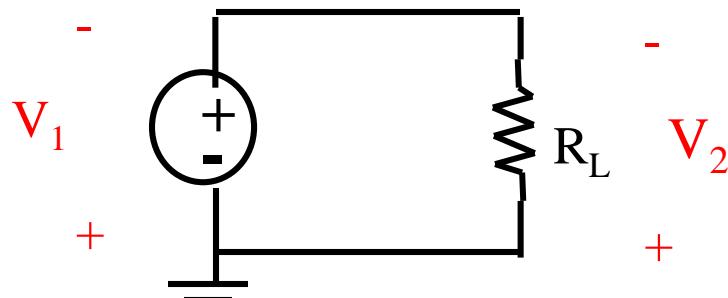


$$\sum V = 0$$

$$V_1 + V_2 = 0$$

$V_1 = (+\text{ve or -ve}) ?$

$V_2 = (+\text{ve or -ve}) ?$

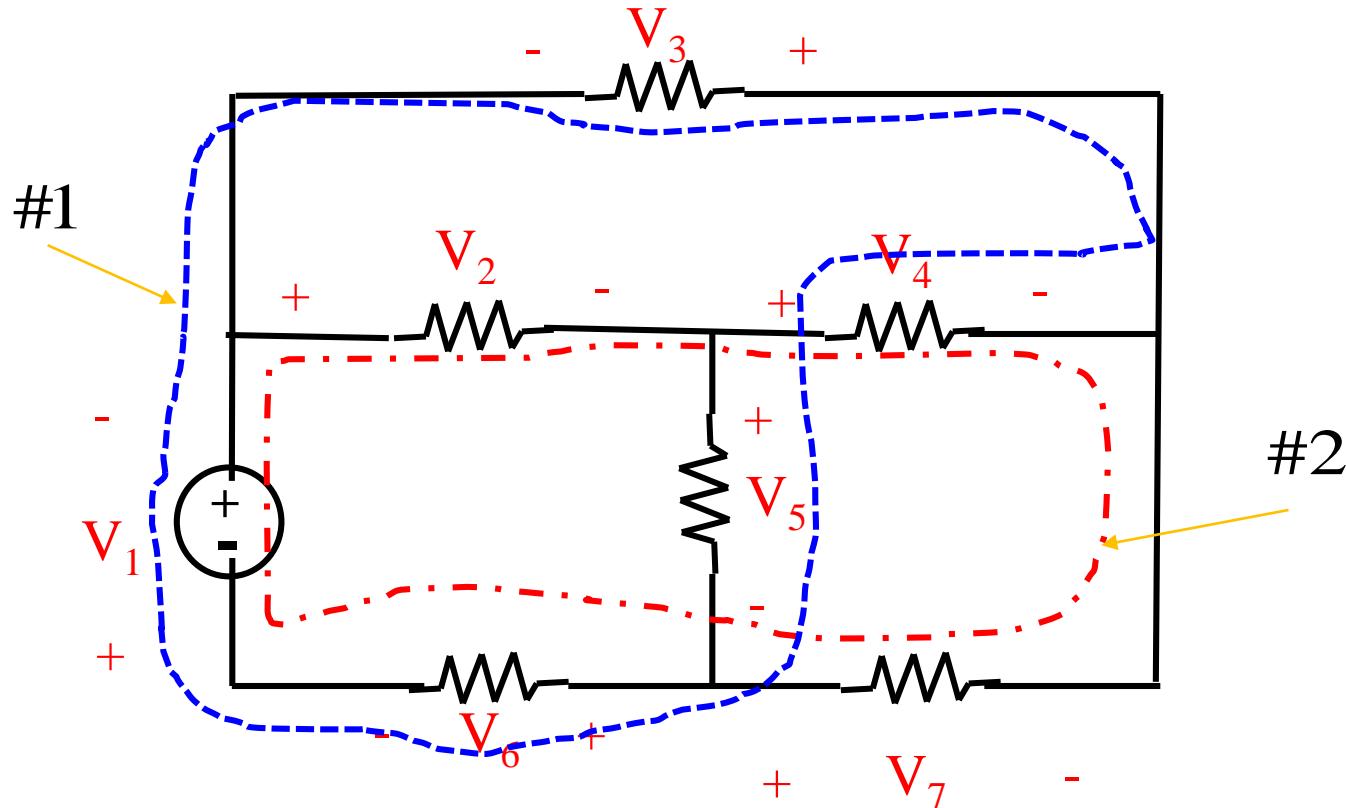


$$\sum V = 0$$

$$(-1)V_1 + V_2 = 0$$

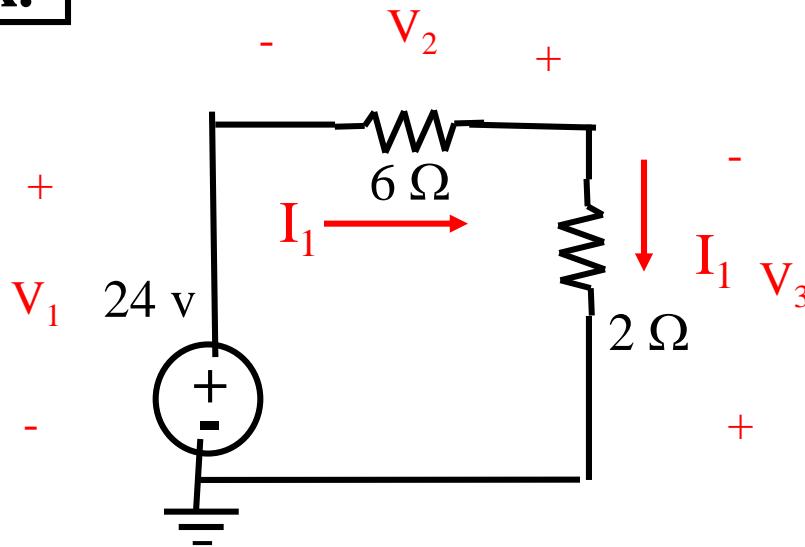
$V_1 = (+\text{ve or -ve}) ?$

$V_2 = (+\text{ve or -ve}) ?$



$$\#1 \quad +(-V_1) + (+V_3) + (+V_4) + (-V_5) + (-V_6) = 0$$

$$\#2 \quad +(-V_1) + (-V_2) + (-V_4) + (+V_7) + (-V_6) = 0$$

Ex.

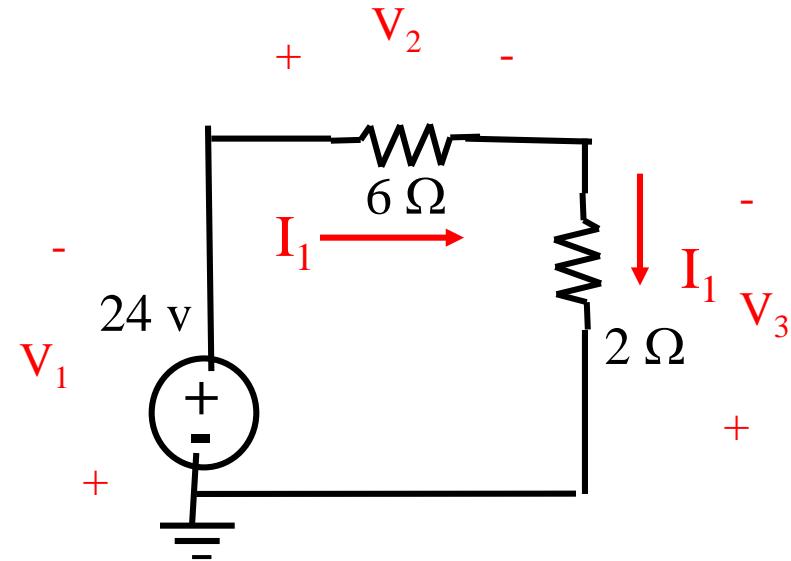
$$\sum V = 0$$

$$\mathbf{V}_1 + \mathbf{V}_2 + \mathbf{V}_3 = 0$$

$$+(24 - 0) + (-I_1)(6) + (-I_1)(2) = 0$$

$$24 = 8 I_1$$

$$I_1 = 3$$



$$\sum V = 0$$

$$(-\mathbf{V}_1) + (-\mathbf{V}_2) + \mathbf{V}_3 = 0$$

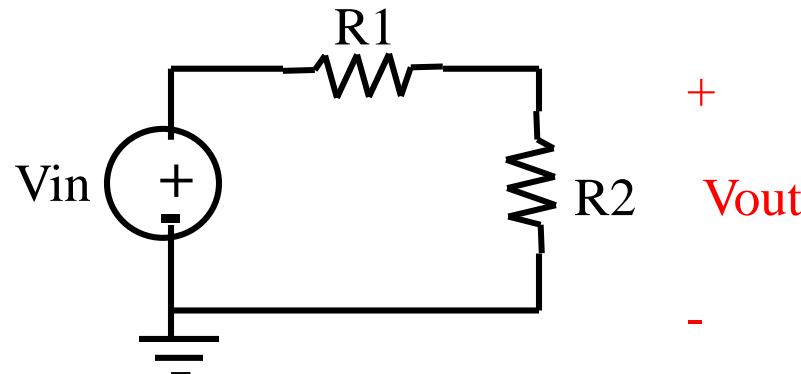
$$+[-(0 - 24)] + [-(I_1)(6)] + (-I_1)(2) = 0$$

$$24 = 8 I_1$$

$$I_1 = 3$$

Useful Equations

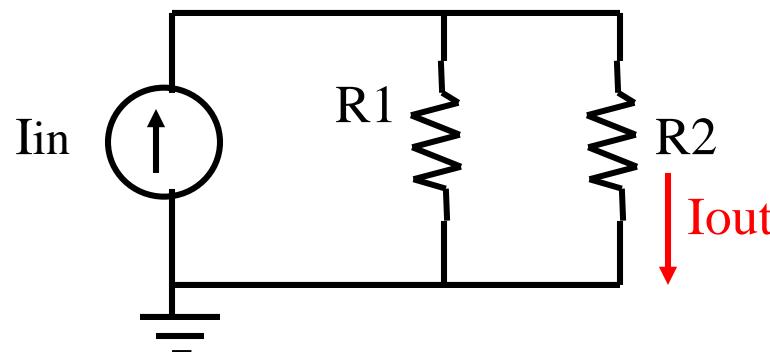
Voltage Divider Circuit



Using KVL

$$V_{out} = \frac{R_2}{R_1 + R_2} V_{in}$$

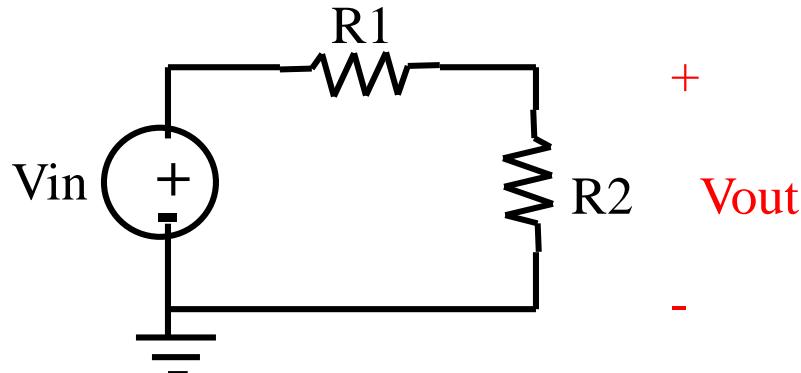
Current Divider Circuit



Using KCL

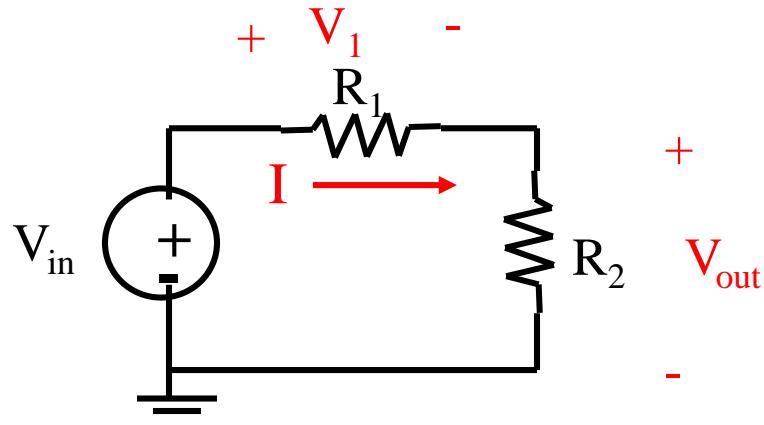
$$I_{out} = \frac{R_1}{R_1 + R_2} I_{in}$$

Voltage Divider Circuit



Using KVL

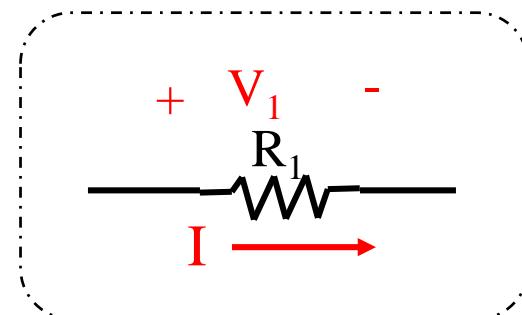
$$V_{out} = \frac{R_2}{R_1 + R_2} V_{in}$$

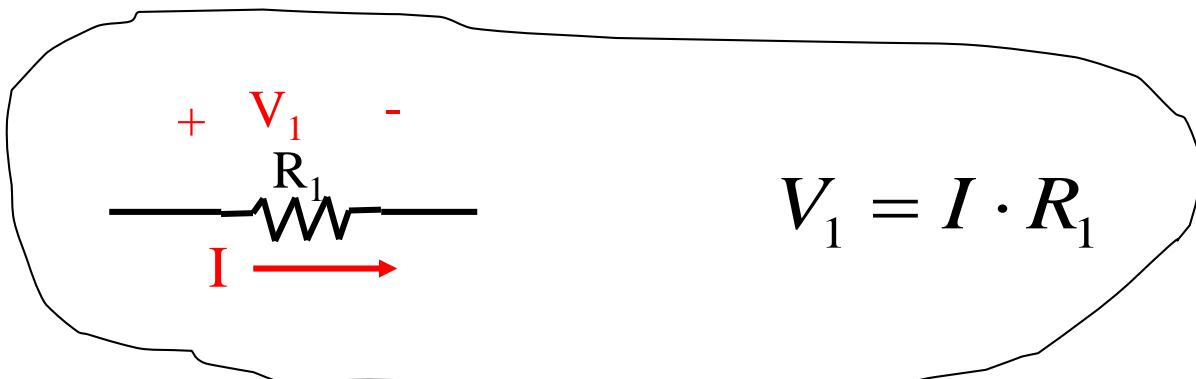


$$\sum V = 0$$

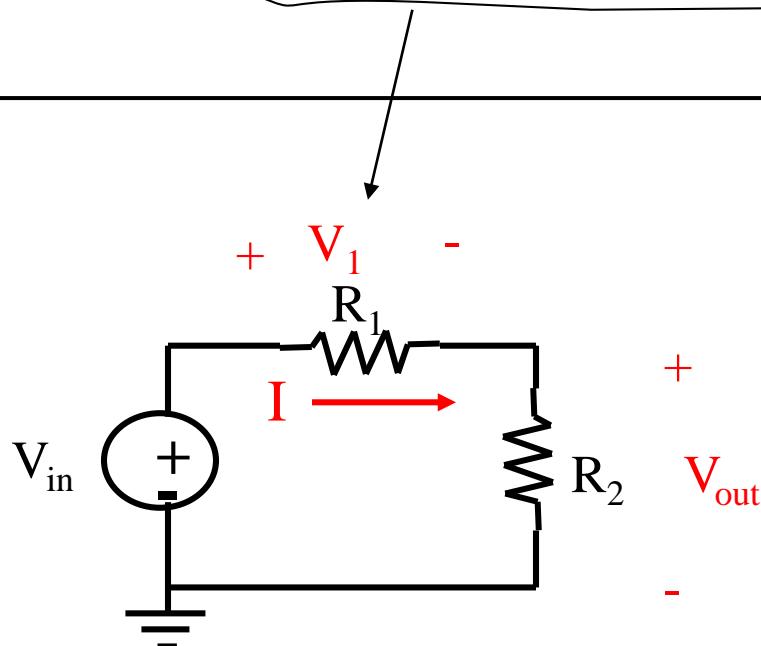
$$V_{in} - V_1 - V_{out} = 0$$

$$V_{out} = V_{in} - V_1$$





$$V_1 = I \cdot R_1$$

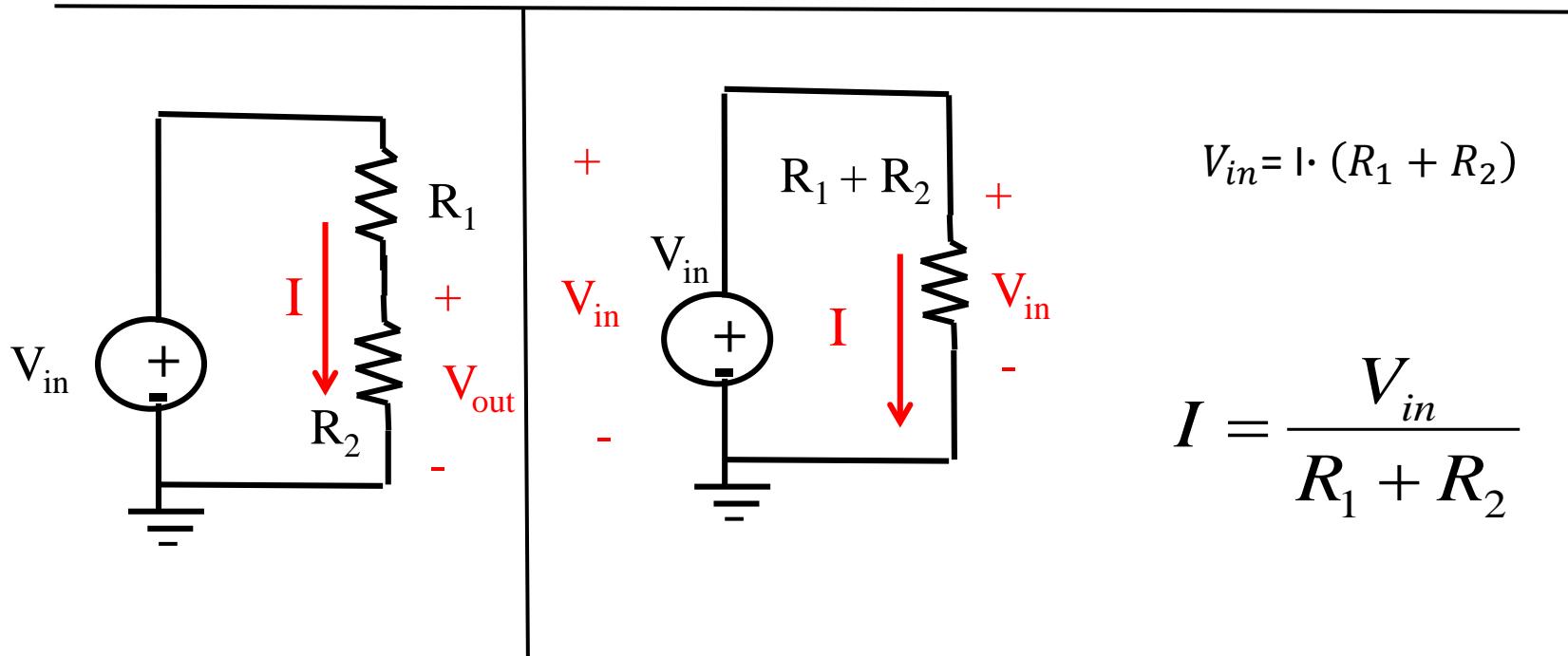
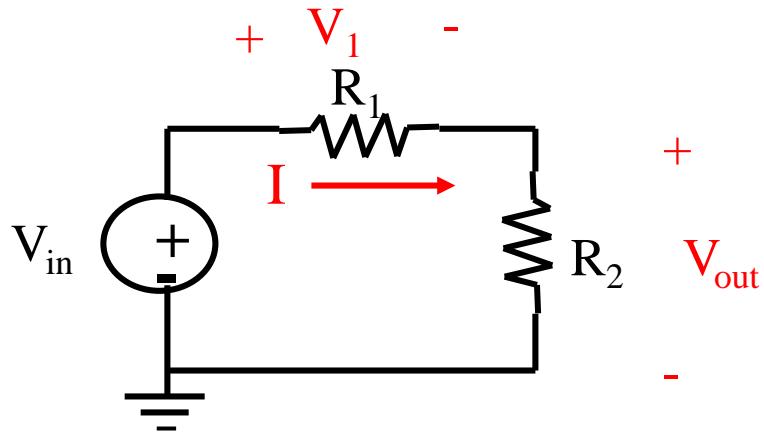


$$\sum V = 0$$

$$V_{in} - V_1 - V_{out} = 0$$

$$V_{out} = V_{in} - V_1$$

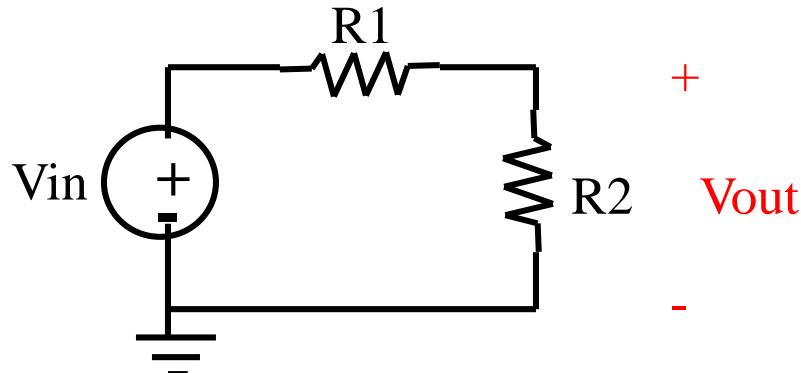
$$V_{out} = V_{in} - I \cdot R_1$$



$$V_{in} = I \cdot (R_1 + R_2)$$

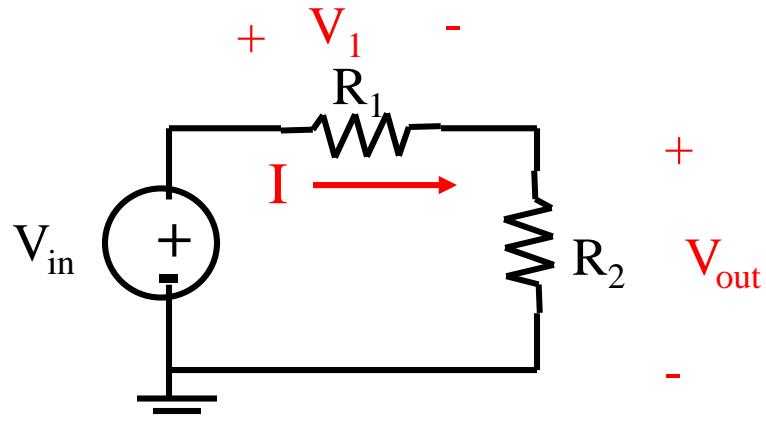
$$I = \frac{V_{in}}{R_1 + R_2}$$

Voltage Divider Circuit



Using KVL

$$V_{out} = \frac{R_2}{R_1 + R_2} V_{in}$$



$$\sum V = 0$$

$$V_{in} - V_1 - V_{out} = 0$$

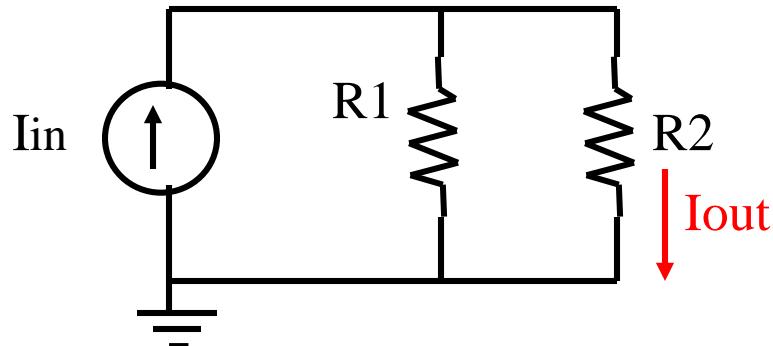
$$V_{out} = V_{in} - V_1$$

$$V_{out} = V_{in} - I \cdot R_1$$

$$V_{out} = V_{in} - \left(\frac{V_{in}}{R_1 + R_2} \right) \cdot R_1$$

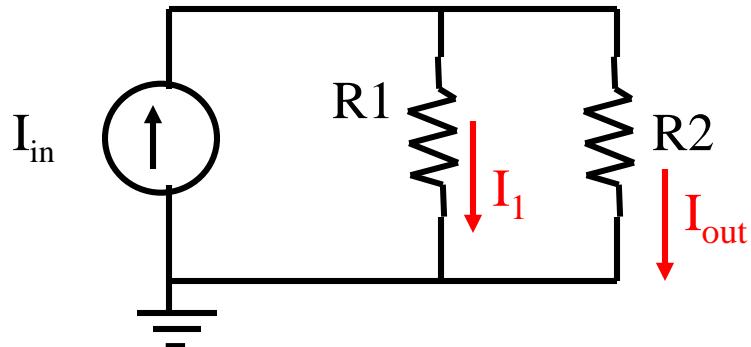
$$V_{out} = \left(\frac{R_2}{R_1 + R_2} \right) \cdot V_{in}$$

Current Divider Circuit



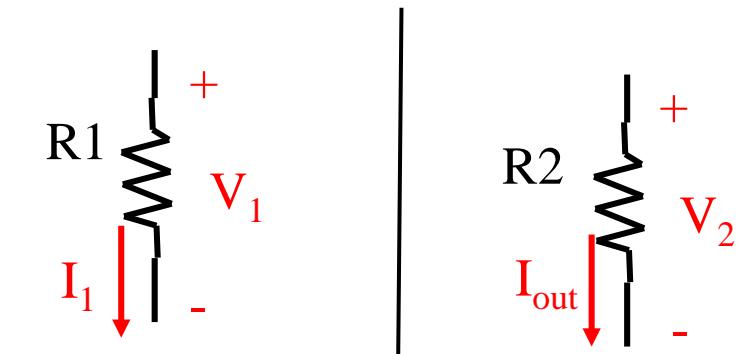
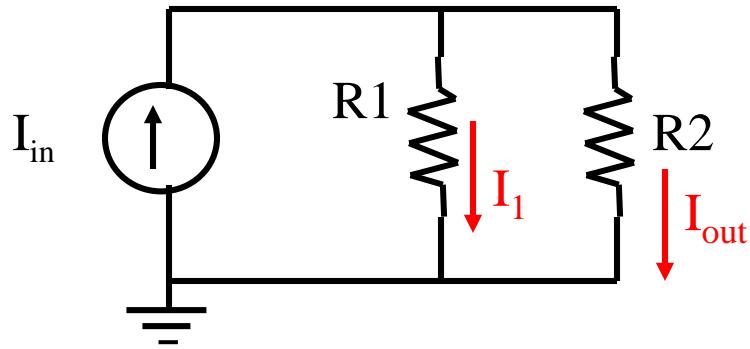
Using KCL

$$I_{out} = \frac{R_1}{R_1 + R_2} I_{in}$$



$$I_{out} = ?$$

$$\begin{aligned}\sum I &= 0 \\ (I_{in}) + (-I_1) + (-I_{out}) &= 0\end{aligned}$$



$$V_1 = I_1 \cdot R1$$

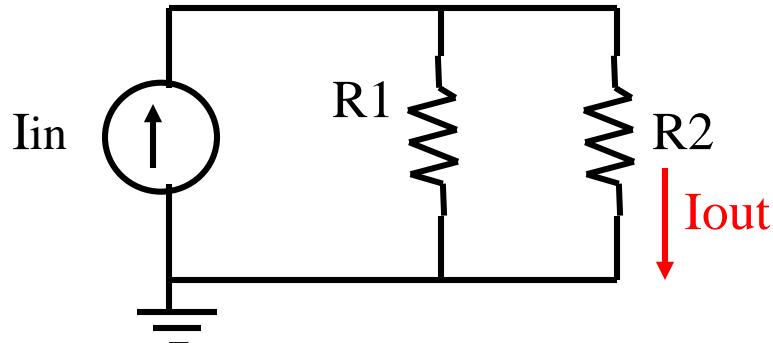
$$V_2 = I_{out} \cdot R2$$

$$V_1 = V_2$$

$$\mathbf{I}_1 \cdot \mathbf{R1} = \mathbf{I}_{out} \cdot \mathbf{R2}$$

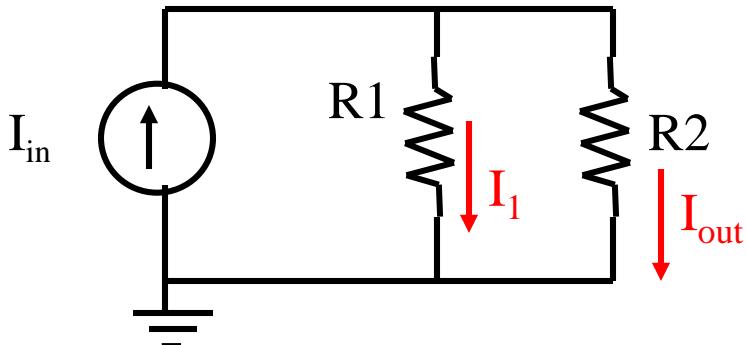
$$\mathbf{I}_1 = \frac{\mathbf{I}_{out} \cdot \mathbf{R2}}{\mathbf{R1}}$$

Current Divider Circuit



Using KCL

$$I_{out} = \frac{R_1}{R_1 + R_2} I_{in}$$



$$I_{out} = ?$$

$$\sum I = 0$$

$$(I_{in}) + (-I_1) + (-I_{out}) = 0$$

$$(I_{in}) + \left(-\frac{I_{out} \cdot R_2}{R_1} \right) + (-I_{out}) = 0$$

$$I_{out} = \frac{R_1}{R_1 + R_2} I_{in}$$